

Douglas Quadling and Julian Gilbey

Cambridge International
AS and A Level Mathematics:

Mechanics 1

Coursebook

Revised Edition

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Cambridge qualifications

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